

Schedule Table Generation for Time-Triggered Mixed Criticality Systems

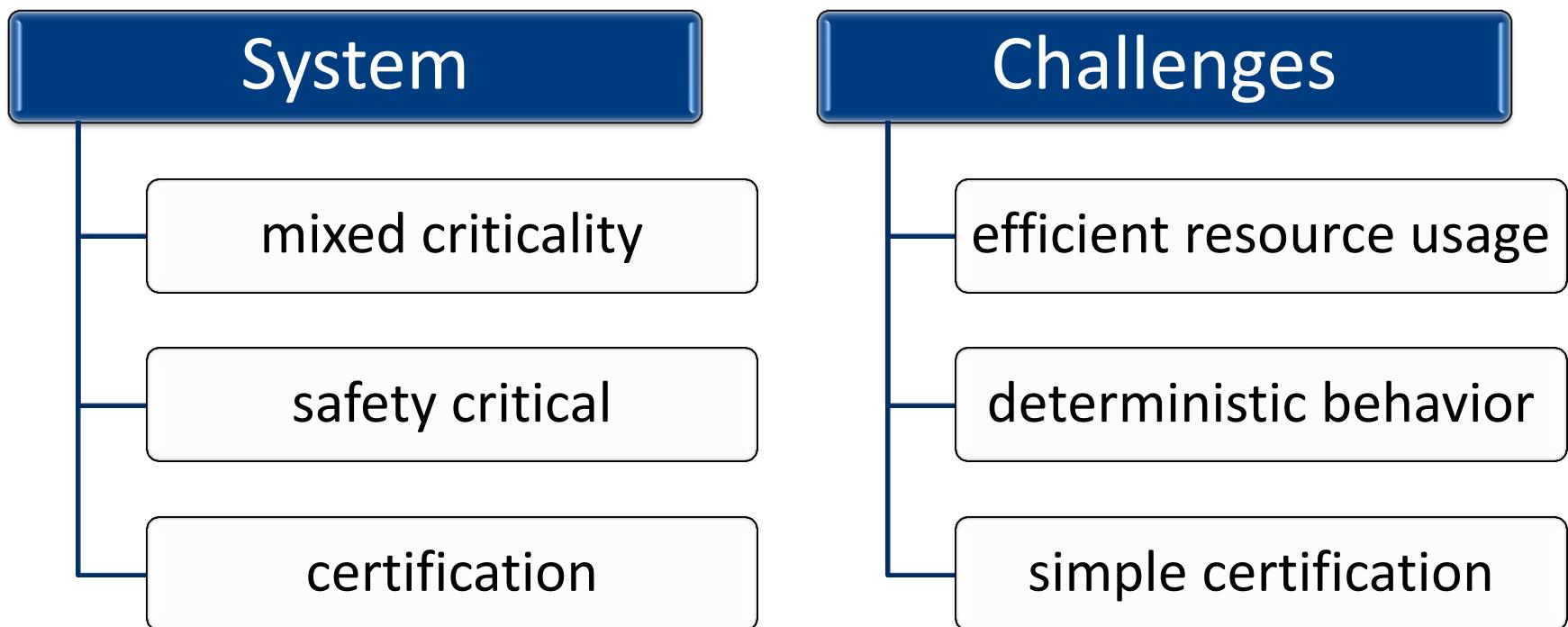
Jens Theis and Gerhard Fohler

Technische Universität Kaiserslautern,
Germany

Sanjoy Baruah

The University of North Carolina,
Chapel Hill, NC, USA

Introduction



Job Model

Vestal-model for dual criticality jobs

r_i release time

d_i deadline

$\chi_i \in \{\text{LO, HI}\}$ criticality levels

$C_i(\text{LO}), C_i(\text{HI})$ worst case execution time (WCET) for LO and HI

$C_i(\text{LO}) = C_i(\text{HI})$, if $\chi_i = \text{LO}$

$C_i(\text{LO}) \leq C_i(\text{HI})$, if $\chi_i = \text{HI}$

→ under certification authorities' (CAs) assumptions

→ under designers' assumptions

Time-Triggered (TT) Mode Changes

- approach by Baruah and Fohler – proof of concept

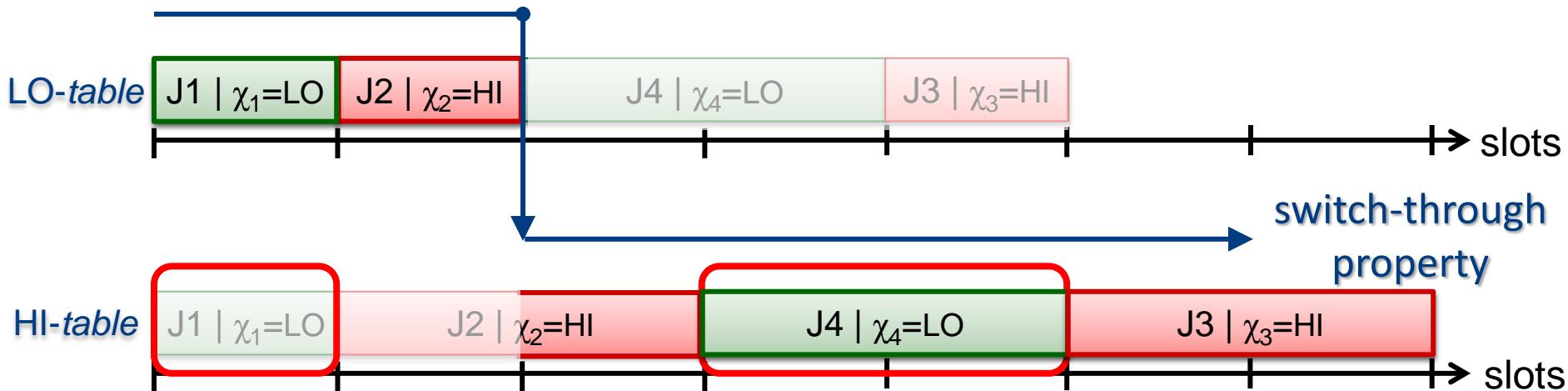
TT schedule tables:



TT Mode Changes

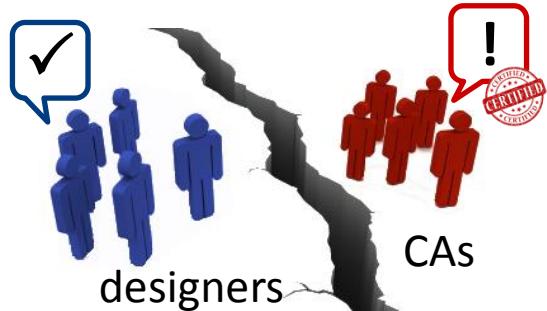
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mode switch at runtime:

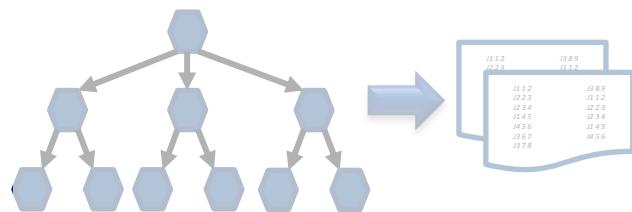


→ switch-through obtained by inserting LO-criticality jobs in HI-table
at cost of utilization

Basic Idea



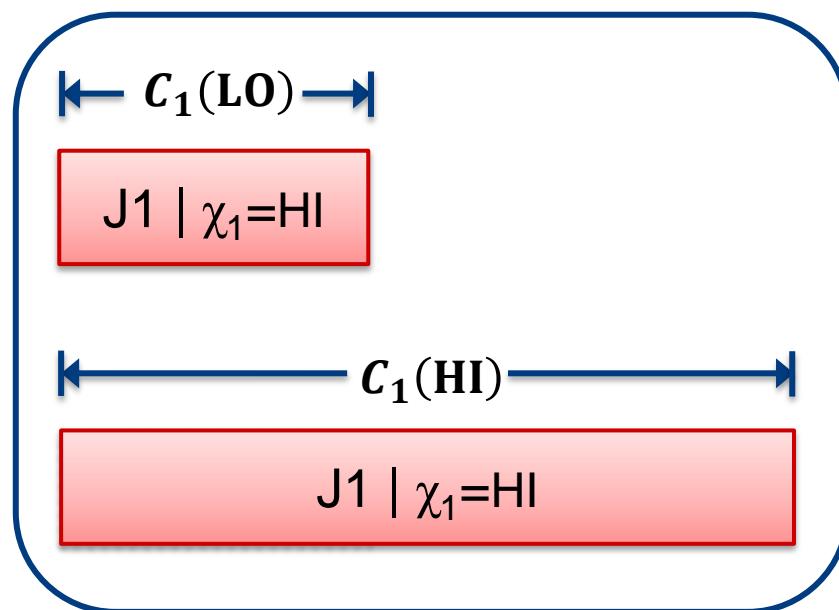
**separate designers' and CAs'
WCET-assumptions**



**use heuristic tree search
to generate two time-triggered (TT)
schedule tables**

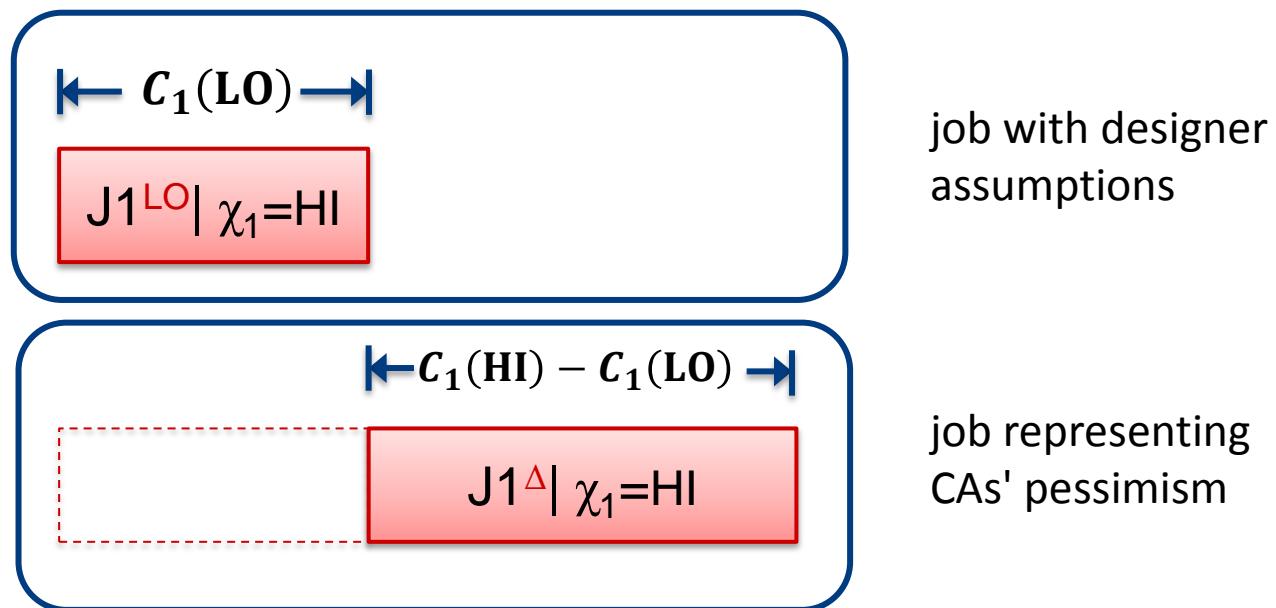
Separate WCET Assumptions

- separate demand based on designer assumptions from additional demand by CAs' pessimism
→ split HI-criticality jobs



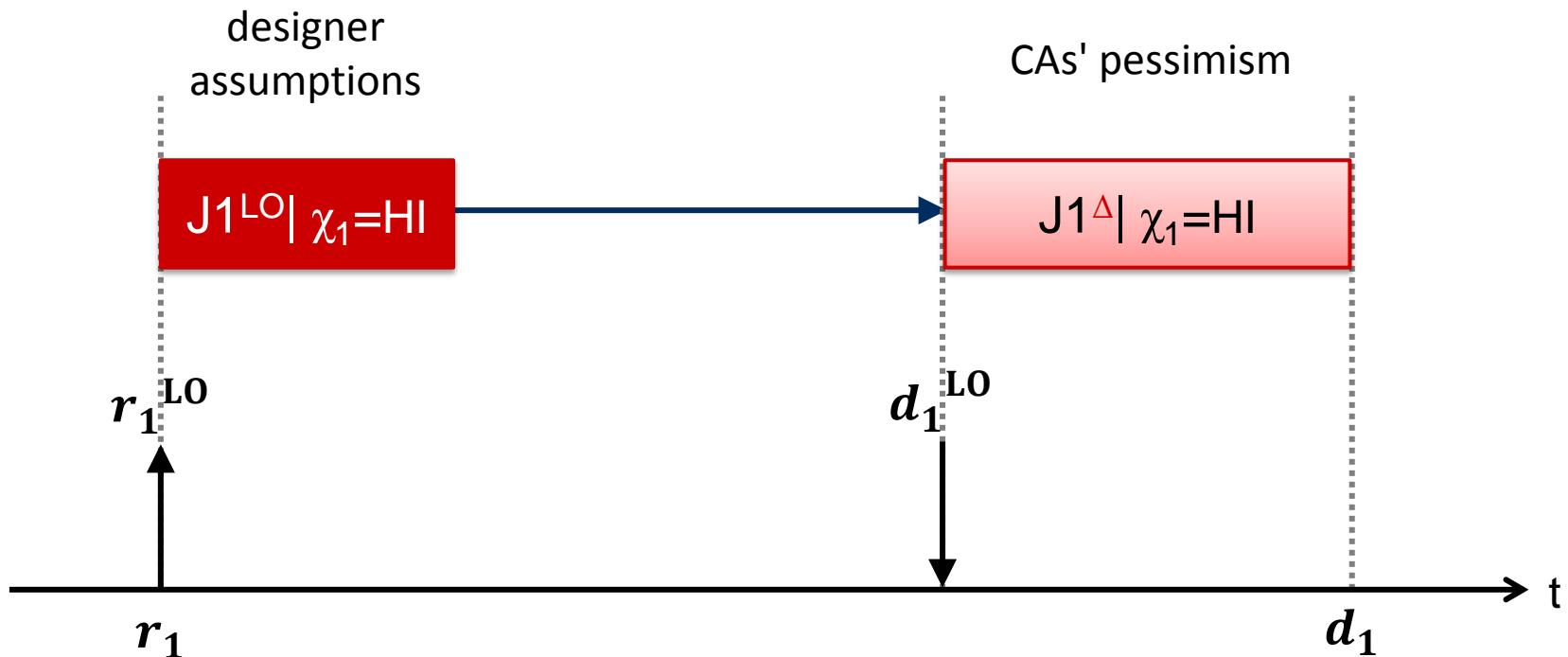
Separate WCET Assumptions

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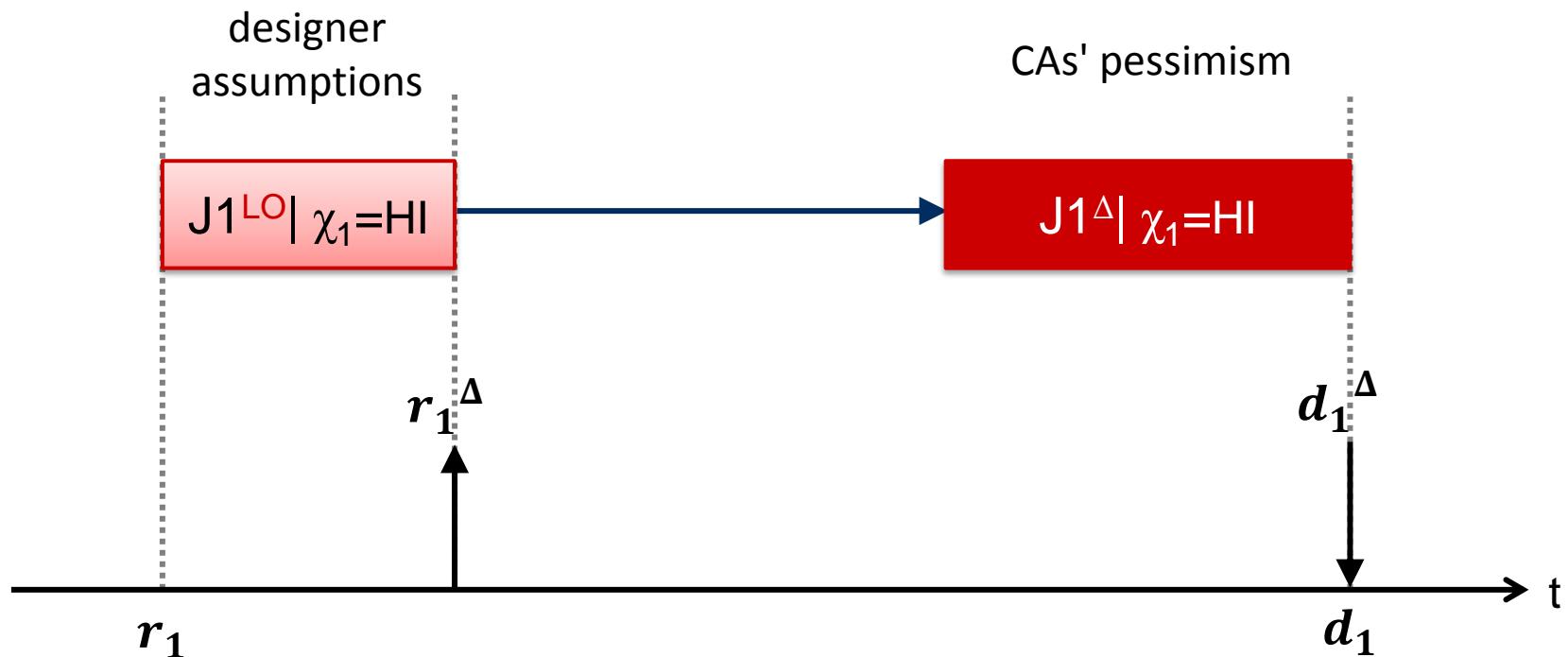
Parameter Derivation of Split Jobs

- add a precedence constraint
- derive new parameters for the split jobs



Parameter Derivation of Split Jobs

- add a precedence constraint
- derive new parameters for the split jobs



Job Parameters Overview

- job parameters for scheduling:

for all jobs with $\chi_i = \text{LO}$:

$$J_i = \langle r_i, d_i, C_i(\text{LO}) \rangle$$

for all jobs with $\chi_i = \text{HI}$:

$$\begin{cases} J_i^{\text{LO}} = \langle r_i^{\text{LO}}, d_i^{\text{LO}}, C_i^{\text{LO}}(\text{LO}) \rangle \\ J_i^{\Delta} = \langle r_i^{\Delta}, d_i^{\Delta}, C_i^{\Delta}(\text{HI}) \rangle \end{cases}$$

Job Allocation to Modes

- job allocation to modes:

LO-table

$J_i \mid \chi_i = LO$

HI-table

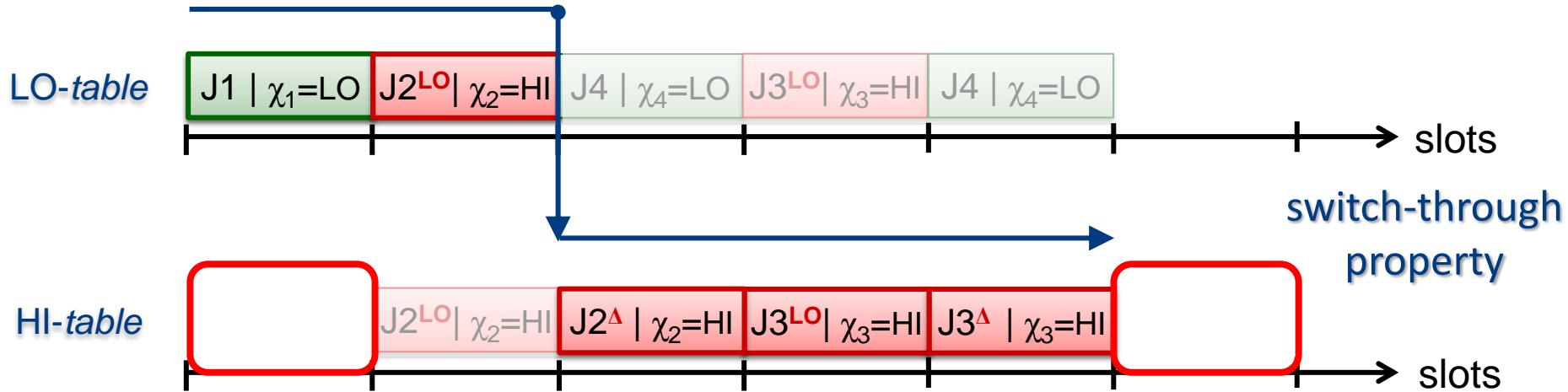
$J_i^{LO} \mid \chi_i = HI$

$J_i^{LO} \mid \chi_i = HI$

$J_i^{\Delta} \mid \chi_i = HI$

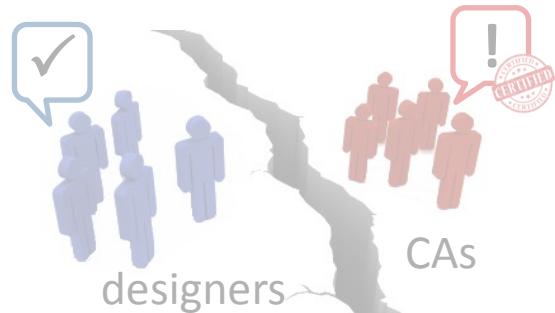
TT Mode Changes after Splitting

- precedence constraints used to reduce utilization in *HI-table*

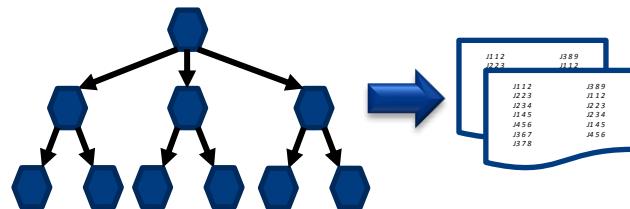


→ switch-through obtained by splitting HI-criticality jobs

Basic Idea



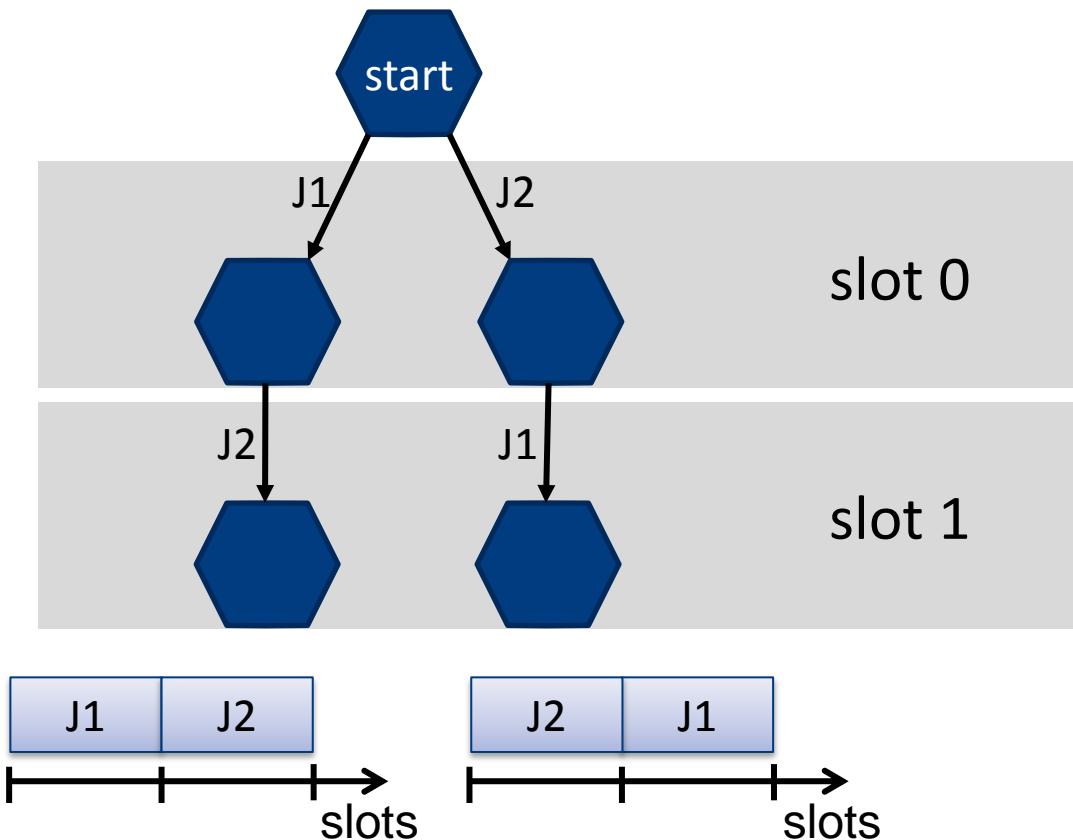
separate designers' and CAs'
WCET-assumptions



use heuristic tree search
to generate two time-triggered (TT)
schedule tables

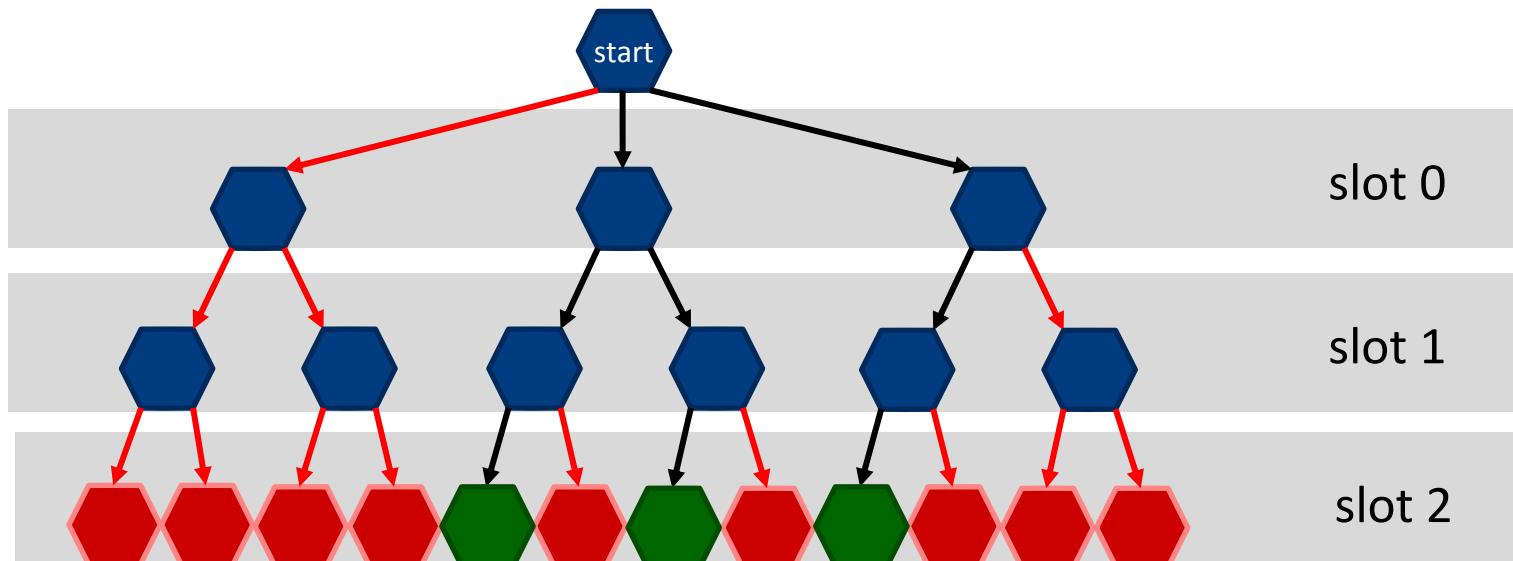
General Tree Search

Example with 2 jobs



Schedule Tables Construction

How can we reduce the search space?



blue hexagon = partial schedule green hexagon = feasible schedule red hexagon = infeasible schedule red arrow = path to infeasible schedule

Guiding the Search

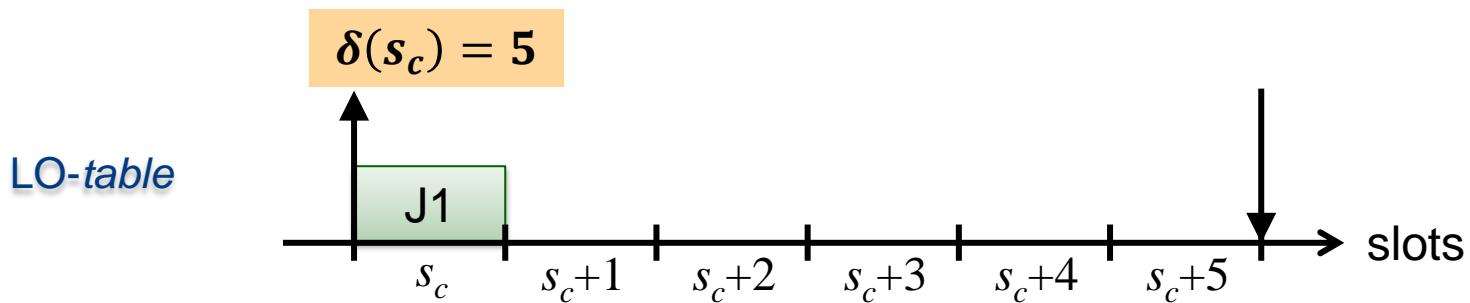
- Heuristic function:

The **leeway $\delta(s)$ of a slot s in LO-table** determines how many slots we can delay the job scheduled in that slot.

- Backtracking

Leeway

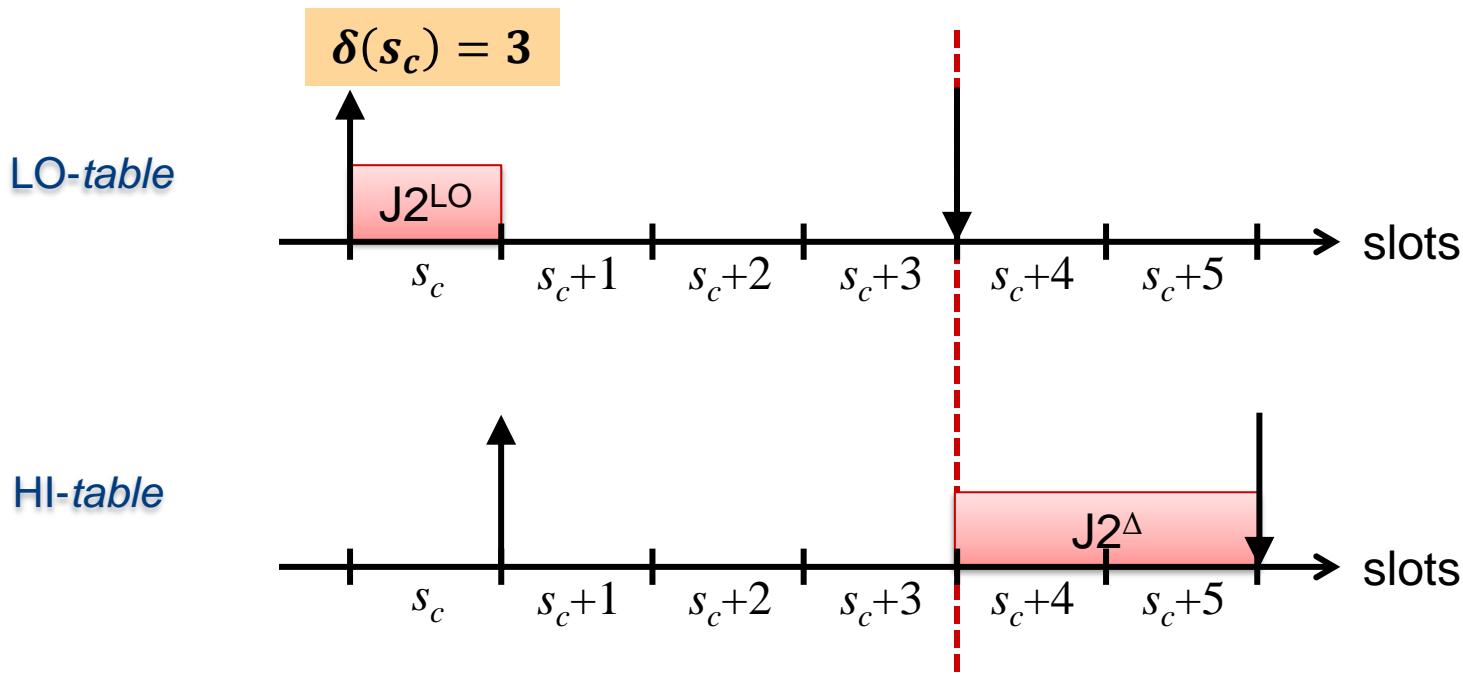
leeway $\delta(s)$ of jobs with $\chi_i = \text{LO}$:



Leeway

leeway $\delta(s)$ of jobs with $\chi_i = \text{HI}$:

(more details considering several HI-criticality jobs in the paper)



Schedule Tables Generation

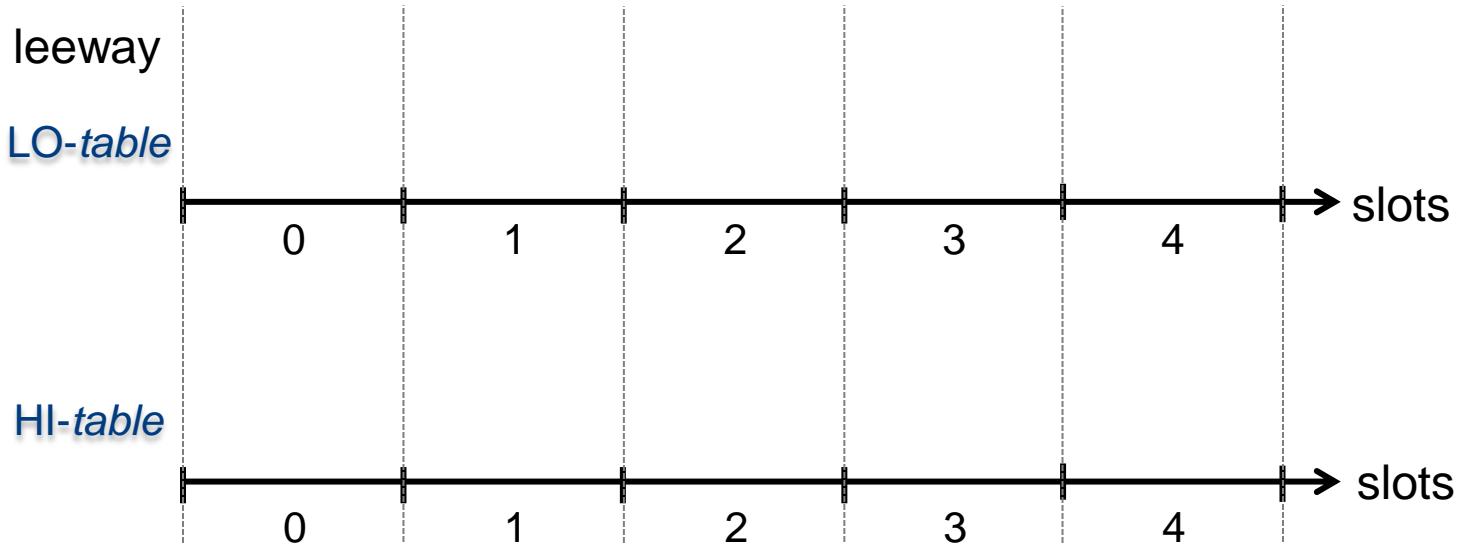
search tree



LO-table: according to EDF

HI-table: depending on criticality level in *LO-table*

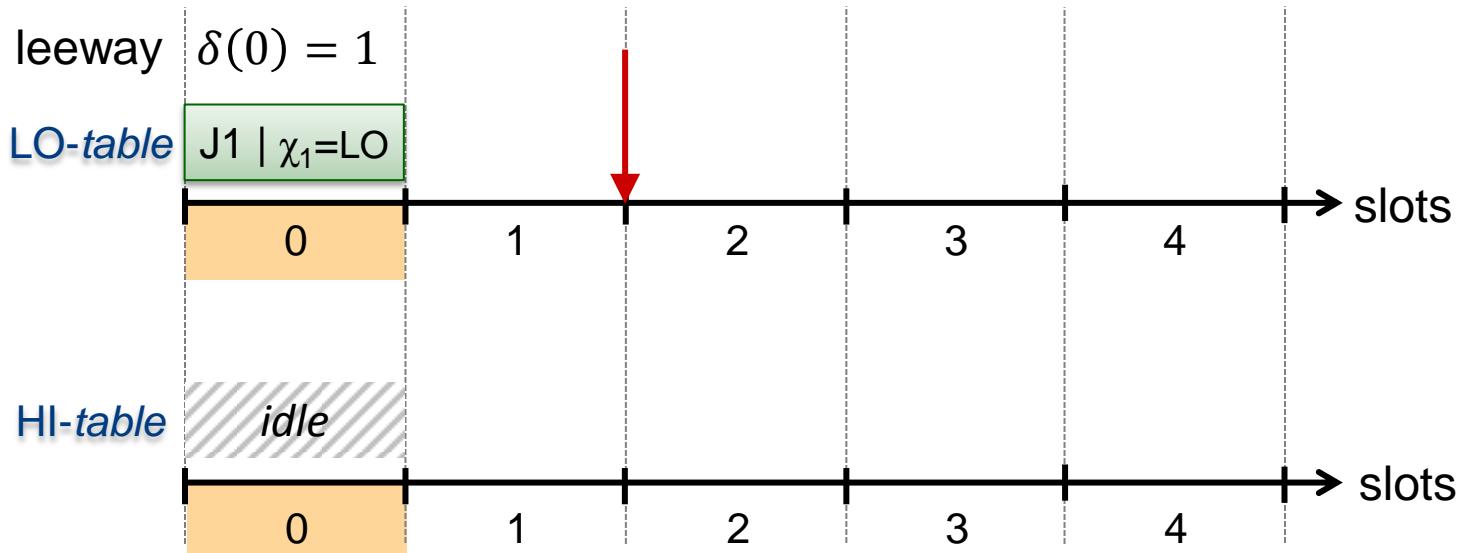
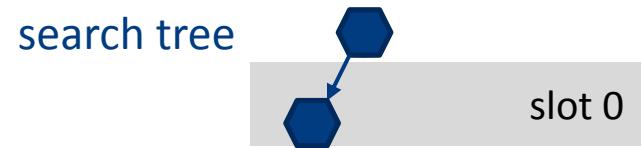
- LO: Δ -fraction job by EDF
- HI: same job as in *LO-table*



Schedule Tables Generation

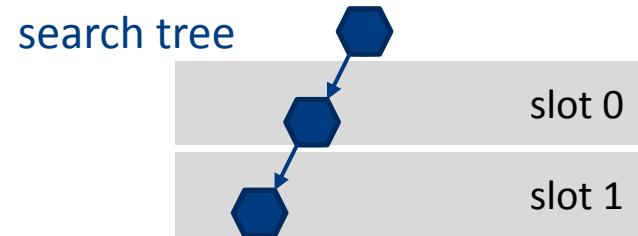
LO-table: select job by EDF
→ J1

HI-table: select Δ -fraction job by EDF
→ idle slot

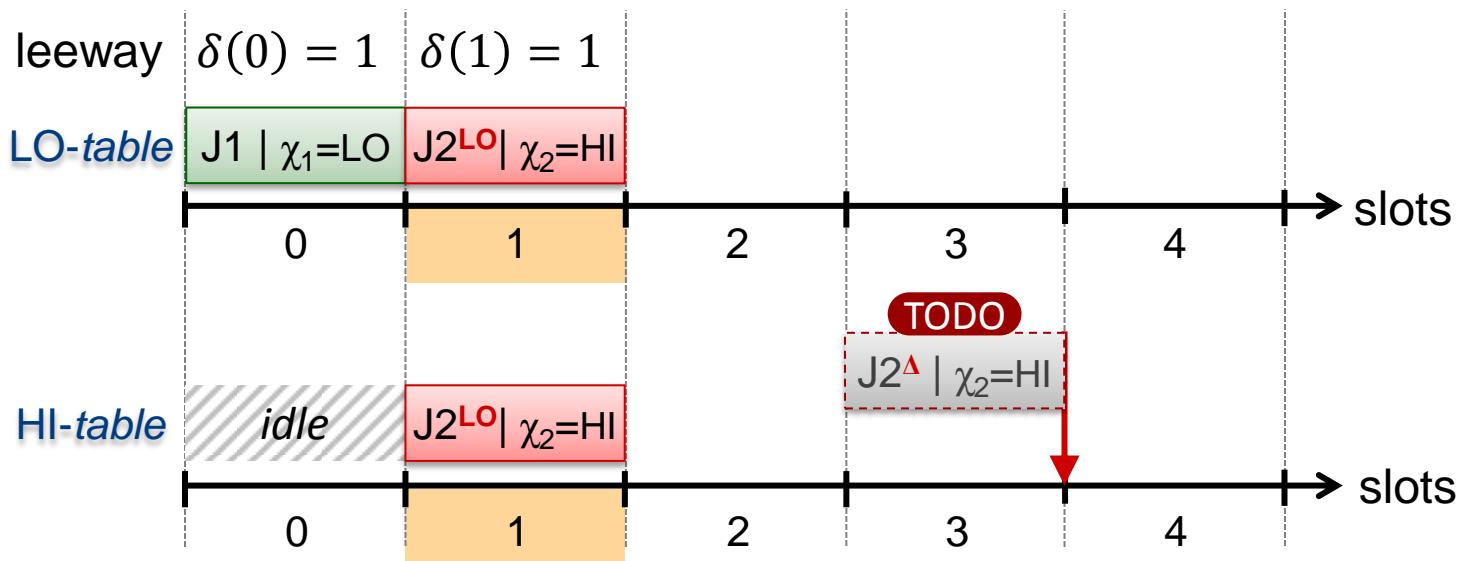


Schedule Tables Generation

LO-table: select job by EDF
→ $J2^{\text{LO}}$



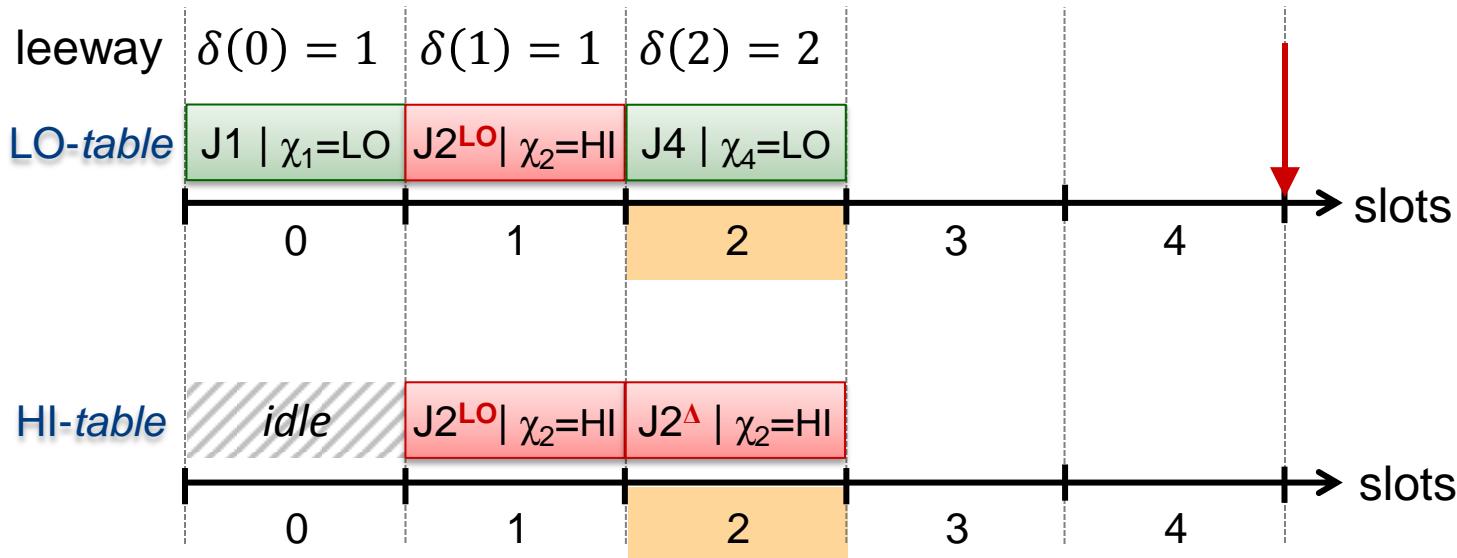
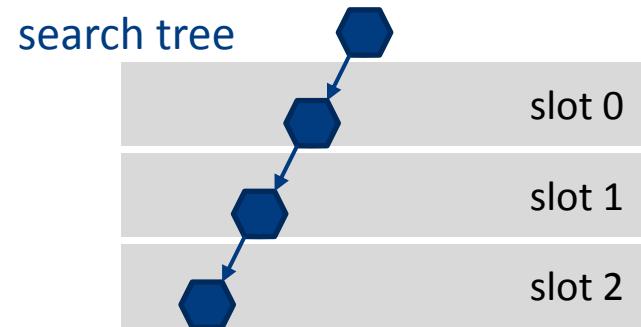
HI-table: schedule same job as in LO-table
→ $J2^{\text{LO}}$



Schedule Tables Generation

LO-table: select job by EDF
 $\rightarrow J4$

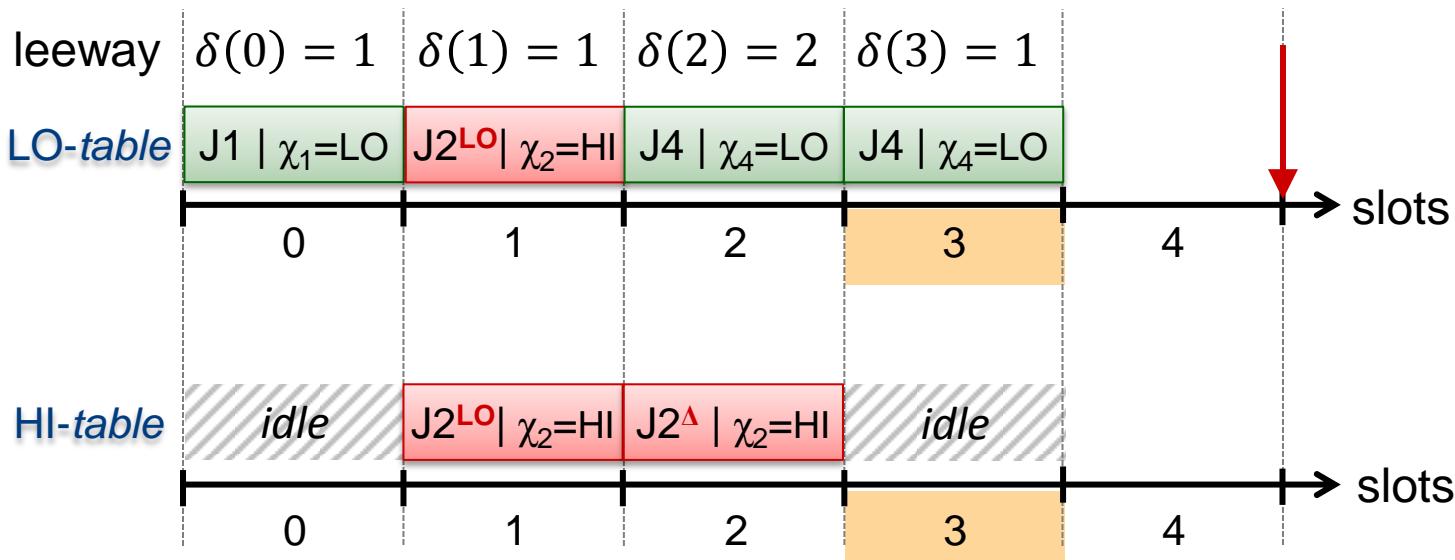
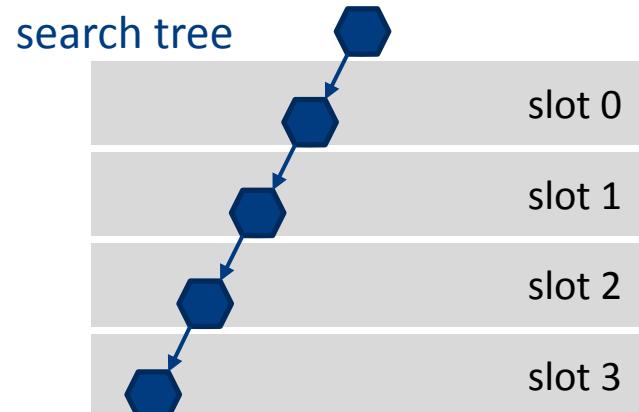
HI-table: select Δ -fraction job by EDF
 $\rightarrow J2^\Delta$



Schedule Tables Generation

LO-table: select job by EDF
 $\rightarrow J4$

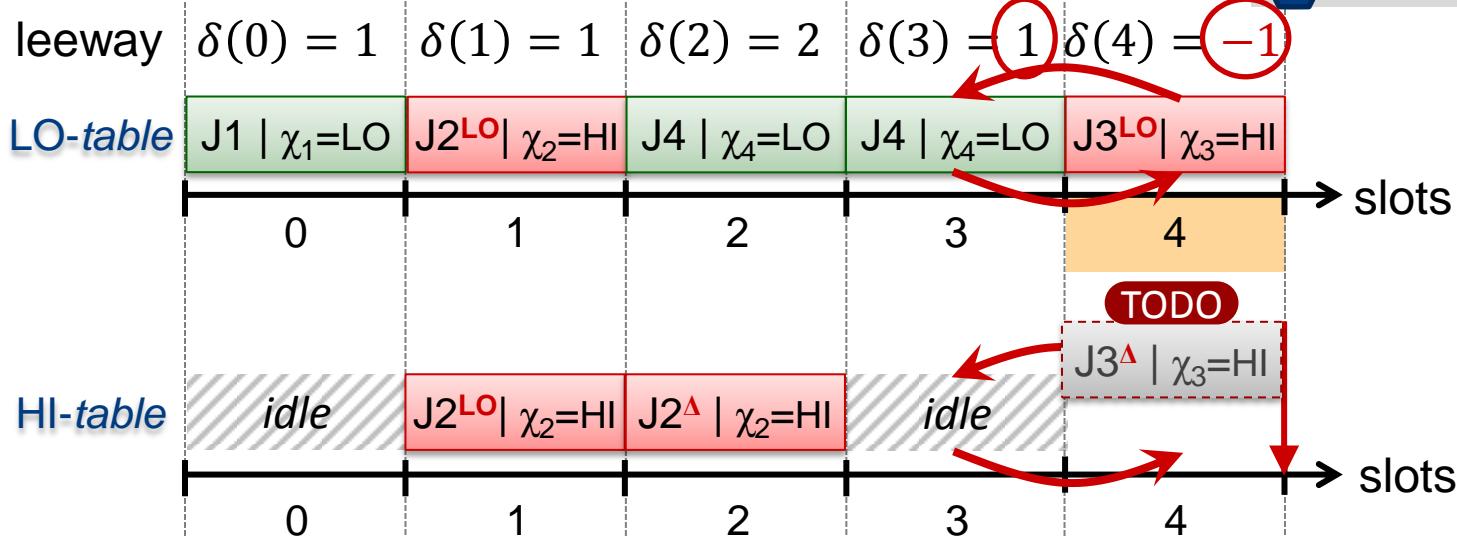
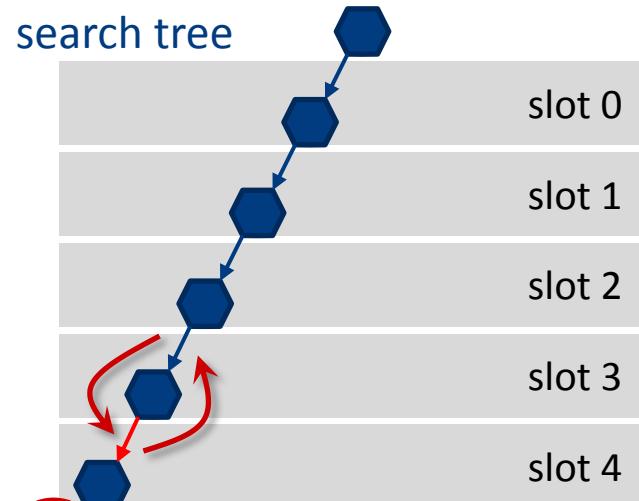
HI-table: select Δ -fraction job by EDF
 \rightarrow idle slot



Schedule Tables Generation

LO-table: select job by EDF
 $\rightarrow J3^{\text{LO}}$

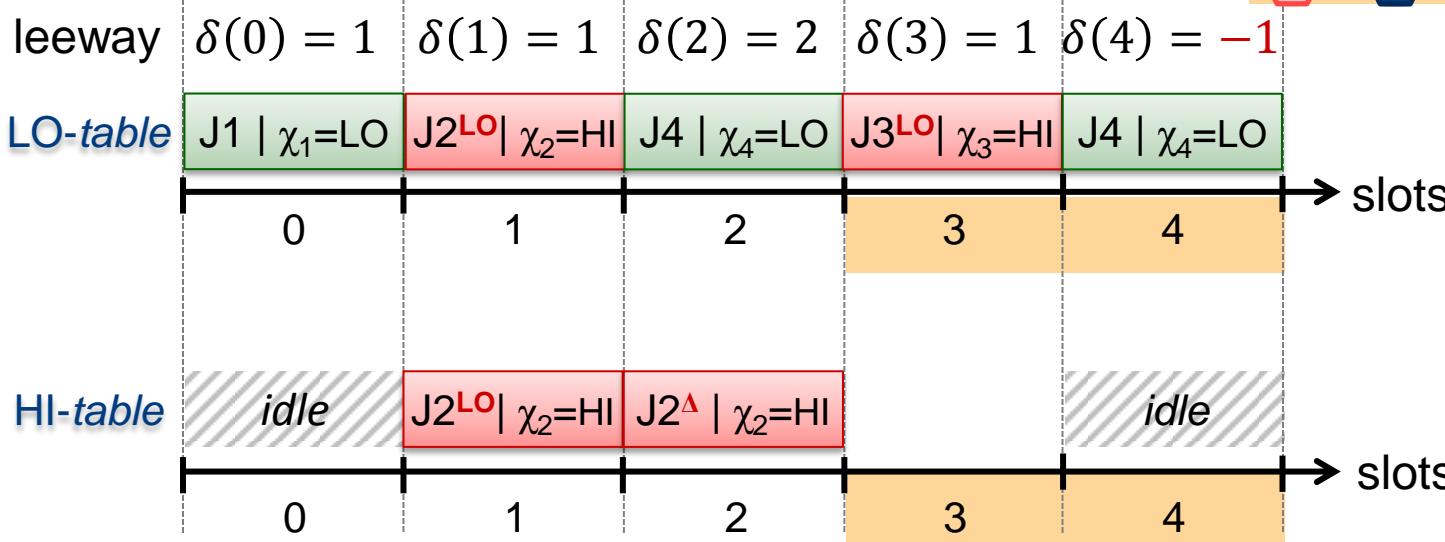
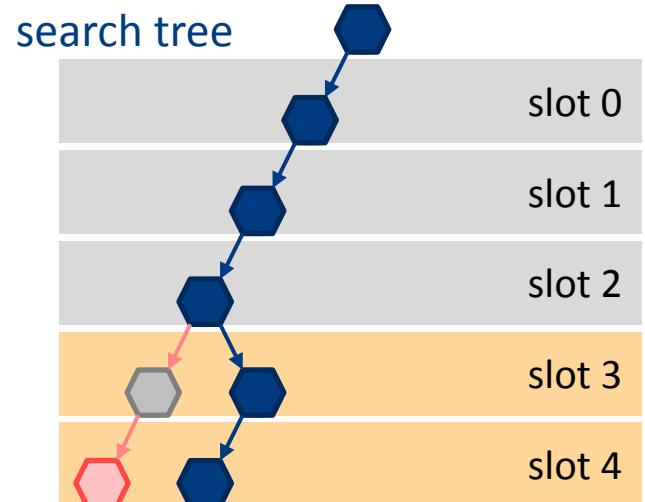
negative leeway \rightarrow backtracking



Schedule Tables Generation

LO-table: select job by EDF
 $\rightarrow J3^{\text{LO}}$

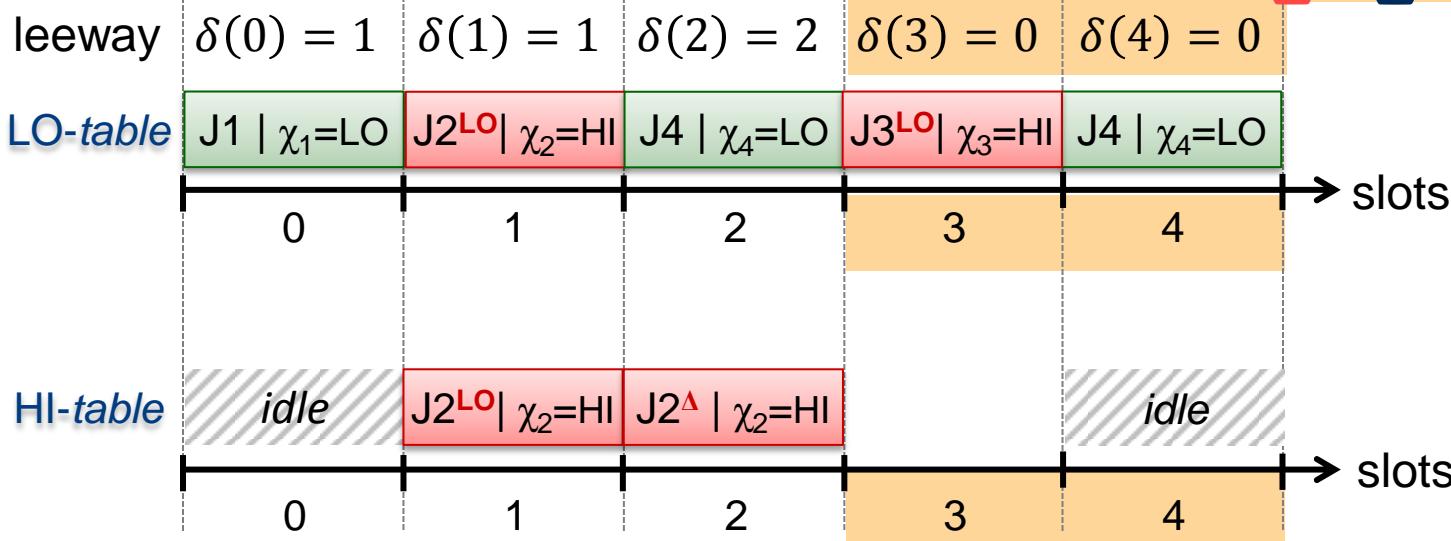
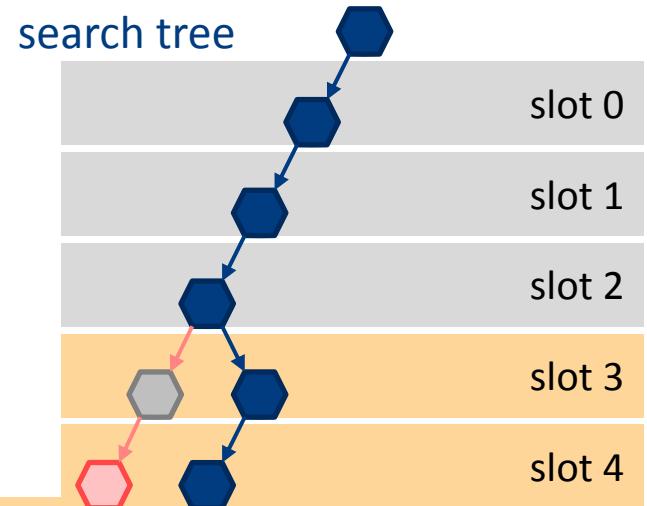
negative leeway \rightarrow backtracking



Schedule Tables Generation

LO-table: select job by EDF
 $\rightarrow J3^{\text{LO}}$

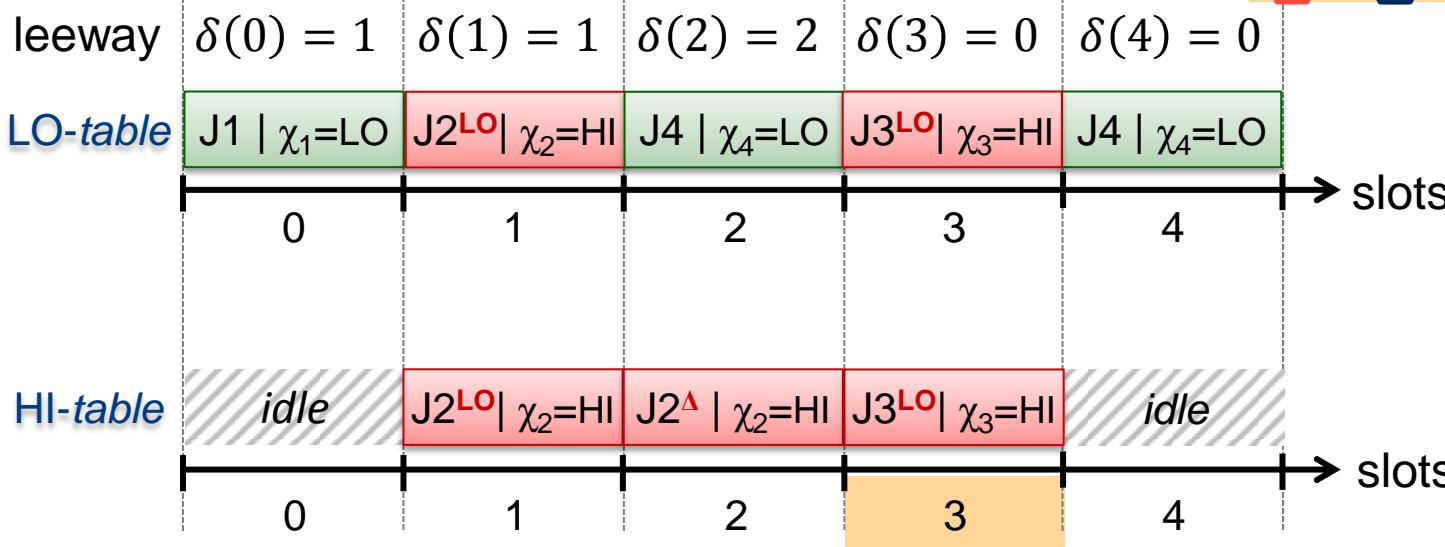
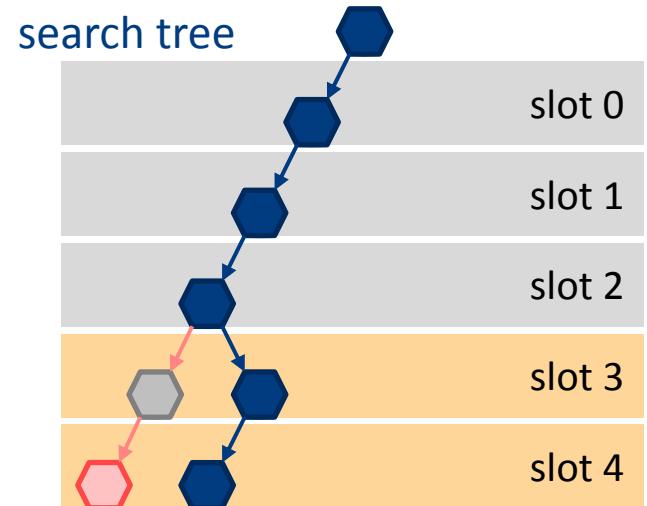
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Schedule Tables Generation

LO-table: select job by EDF
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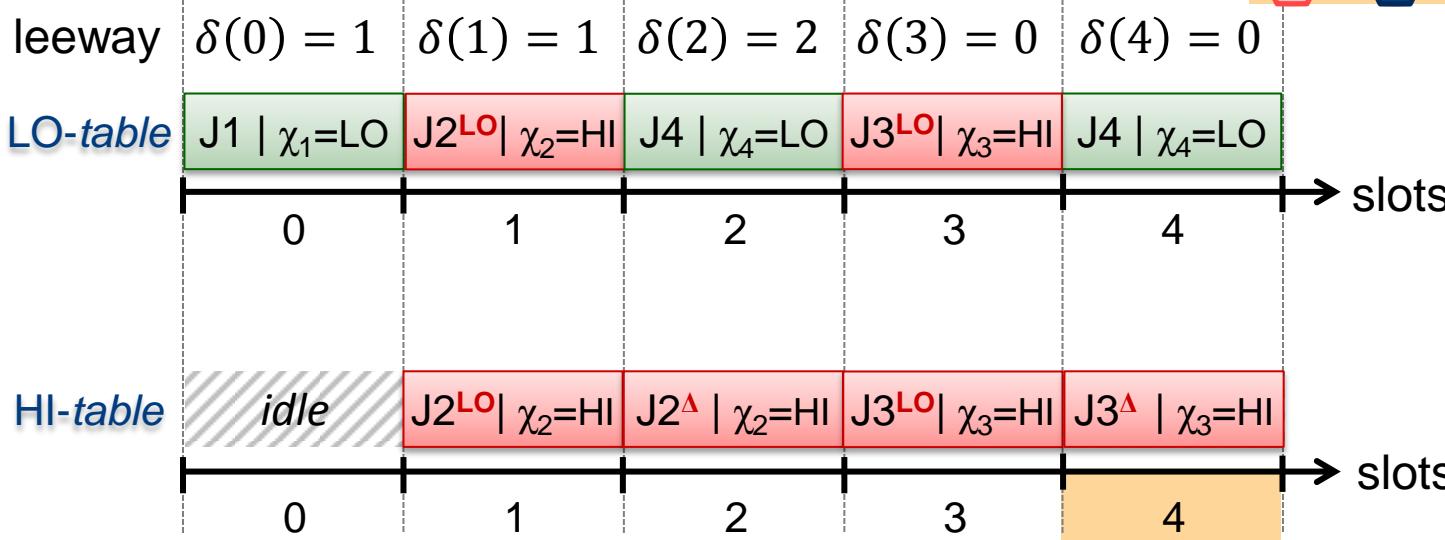
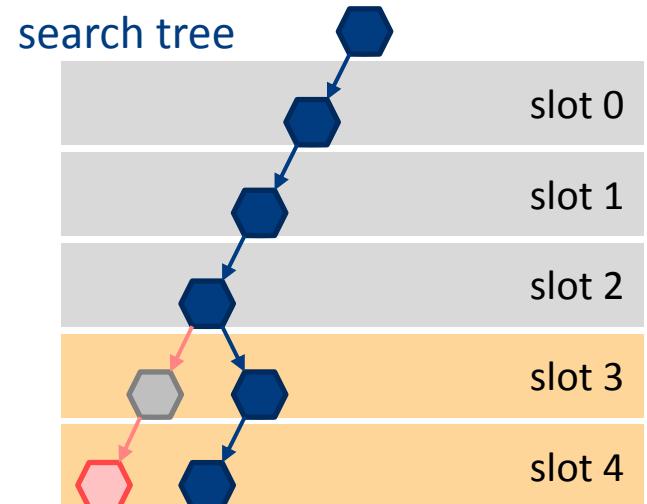
HI-table: schedule same job as in LO-table
 $\rightarrow J3^{\text{LO}}$



Schedule Tables Generation

LO-table: swapped job has LO-criticality

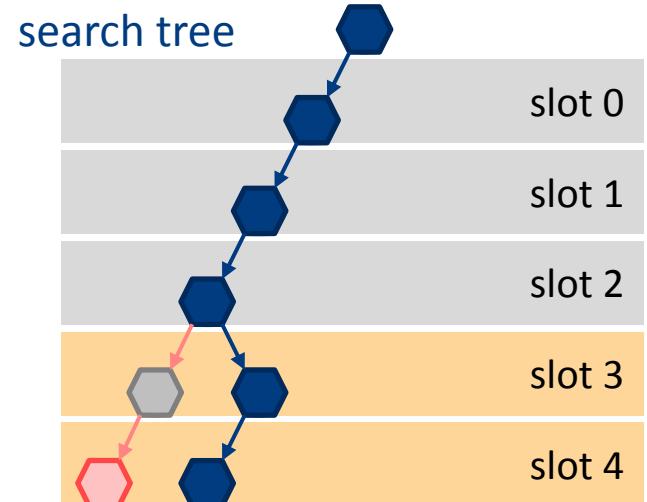
HI-table: select Δ -fraction job by EDF
 $\rightarrow J3^\Delta$



Schedule Tables Generation

LO-table: swapped job has LO-criticality

HI-table: select Δ -fraction job by EDF
 $\rightarrow J3^\Delta$



leeway $\delta(0) = 1 \quad \delta(1) = 1 \quad \delta(2) = 2 \quad \delta(3) = 0 \quad \delta(4) = 0$

LO-table $J1 \mid \chi_1=LO$ $J2^{LO} \mid \chi_2=HI$ $J4 \mid \chi_4=LO$ $J3^{LO} \mid \chi_3=HI$ $J4 \mid \chi_4=LO$

0 1 2 3 4

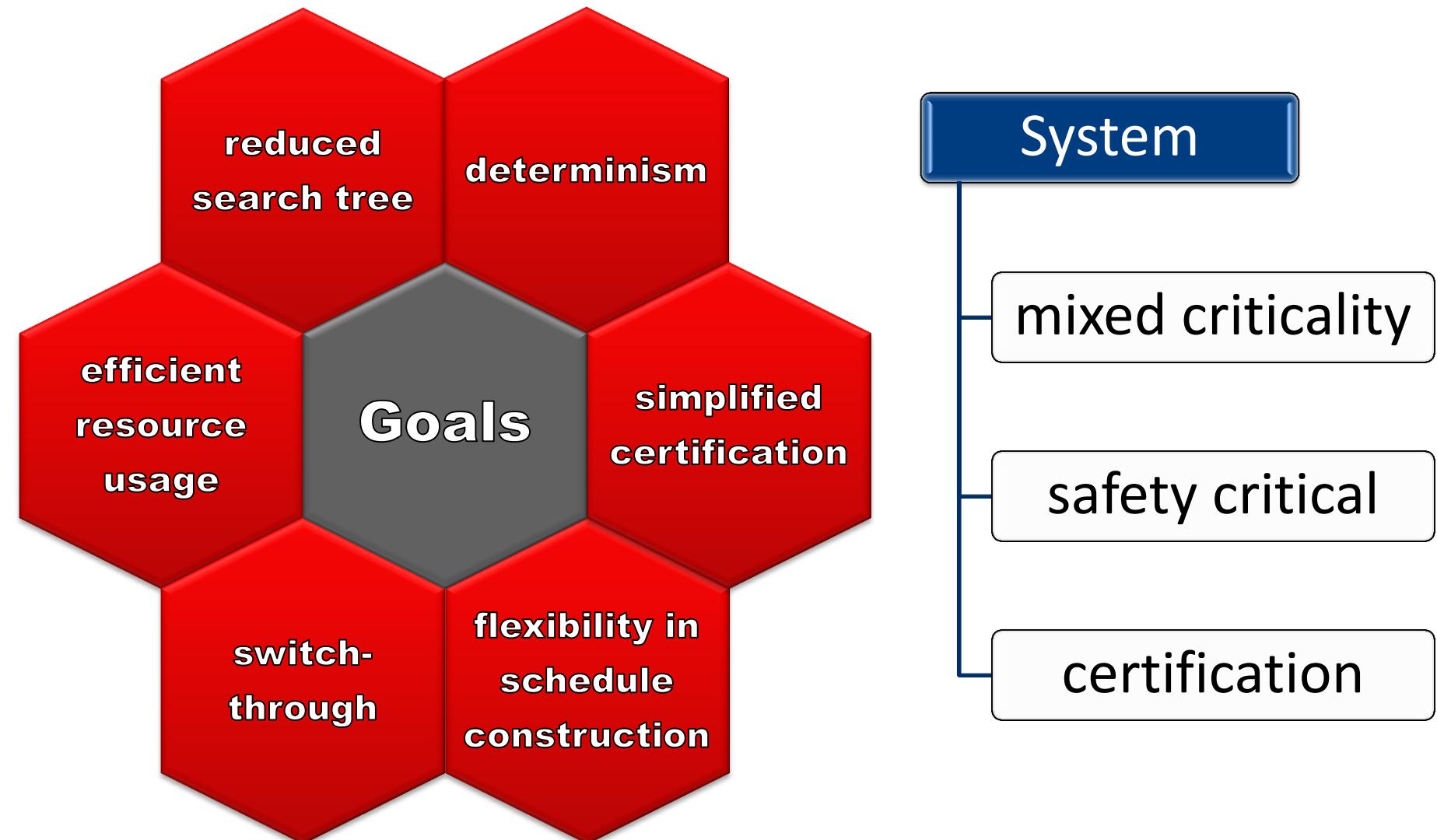
→ slots

HI-table $idle$ $J2^{LO} \mid \chi_2=HI$ $J2^\Delta \mid \chi_2=HI$ $J3^{LO} \mid \chi_3=HI$ $J3^\Delta \mid \chi_3=HI$

0 1 2 3 4

→ slots

Conclusion



Conclusion



- created two TT schedule tables (*one for each criticality level*)
- constructive proof by TT execution
- job splitting separates designer and CAs assumptions
- added precedence constraints
- pessimistic CAs assumptions excluded from LO-criticality system behavior
- *leeway* and *swapping* used for backtracking

Thank You.

Jens Theis and Gerhard Fohler

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